CHAPTER VII

CONCLUSION

In this thesis we have described a 3.5 km interferometer, set up at Ootacamund, for operation at 327 MHz. The Ooty telescope is used as the main element of the interferometer. The electronics for the radio link of the north 13.5 m dish and receiver system for both the north dish and the nearby dish have been completed. Observations of the planet Jupiter, Sgr-A and a few Markarian galaxies are described.

In building the interferometer we have taken advantage of the fact that the Ooty telescope has a long north-south aperture, a large collecting area and a $9\frac{1}{2}$ hour tracking capability. This makes it possible to build an interferometer for synthesizing large aperture by putting several small sized antennas at fixed locations around the Ooty telescope. In the first instance, we have constructed a four-element interferometer by putting three parabolic dishes around the Ooty telescope. The interferometer provides a beam of 40" arc in east-west,3.5 arc in northsouth at declination of zero degree and has a confusion limit of about 25 mJy. Though the existing interferometer has a limited (u, v) coverage it has a low confusion limit and therefore it is well suited for detection of weak radio sources. Besides, it is a useful instrument for the study of

those sources which have almost line brightness distribution and also radio sources at low declinations.

For generating coherent local oscillator signals at element antennas of the interferometer a phase stable radio link based on the sum frequency principle has been built. The radio link works for a one—way path loss of 75 dB. The IF signals from the remote antennas are brought on microwave links.

The interferometer receivers have system temperatures of about 300°K. The correlation receivers use acoustic surface-wave delay lines which have a bandwidth of 2 MHz. In a single $9\frac{1}{2}$ hour observing period the interferometer, consisting of the Ooty telescope and one 13.5 m dish, for a 30 mJy source provides a signal to noise ratio of 5. The rms phase stability of the entire *system* is about 12°.

The present on-line computer program for delay control and data acquisition allows observations of only one baseline at a time. Therefore, the observations of Jupiter were made with the interferometer consisting of the Ooty telescope and the 13.5 m north dish. The observations were mainly in the hour-angle range of 00^h to $+05^h30^m$. W We have obtained strip brightness distributions along the magnetic equator of Jupiter for the three CML ranges, namely 315[°] to 75[°], 75[°] to 195[°] and 195[°] to 315[°], at 327 MHz with a resolution of about 50" arc. Jupiter has been completely resolved along its magnetic equator with two strong peaks

those sources which have almost line brightness distribution and also radio sources at low declinations.

For generating coherent local oscillator signals at element antennas of the interferometer a phase stable radio link based on the sum frequency principle has been built. The radio link works for a one—way path loss of 75 dB. The IF signals from the remote antennas are brought on microwave links.

The interferometer receivers have system temperatures of about 300°K. The correlation receivers use acoustic surface-wave delay lines which have a bandwidth of 2 MHz. In a single $9\frac{1}{2}$ hour observing period the interferometer, consisting of the Ooty telescope and one 13.5 m dish, for a 30 mJy source provides a signal to noise ratio of 5. The rms phase stability of the entire system is about 12[°].

The present on-line computer program for delay control and data acquisition allows observations of only one baseline at a time. Therefore, the observations of Jupiter were made with the interferometer consisting of the Ooty telescope and the 13.5 m north dish. The observations were mainly in the hour-angle range of 00^{h} to $+05^{\text{h}}30^{\text{m}}$. We have obtained strip brightness distributions along the magnetic equator of Jupiter for the three CML ranges, namely 315[°] to 75[°], 75[°] to 195[°] and 195[°] to 315[°], at 327 MHz with a resolution of about 50" arc. Jupiter has been completely resolved along its magnetic equator with two strong peaks

separated by about 3.4 R_{I} . The peaks show asymmetry in their strengths as well as in their location with respect to the centre. Also, the asymmetry varies with the longitude ranges. We have compared the mean brightness distribution over longitude ranges 315° to 75° and 75° to 195° at 92 cm with that obtained from Branson's maps at 21 cm (Branson 1968). The separation between the peaks at 92 cm seems to be slightly larger than that at 21 cm (Branson 1968), though the overall extent of radio emitting region is roughly same at the two wavelengths. We have also obtained the spectral index distribution between 92 cm and 21 cm as a function of radial distance. The spectrum shows a tendency of steepening with radial distance. However, the present observations at 92 cm contain mostly unpolarized radiation because of the north-south orientation of the feeds of the interferometer antennas used. Since Jupiter is strongly polarized the effects due to the above limitation may be significant. It is planned to make further observations with the Ooty interferometer using crossed dipole feeds.

Because of the limited (u,v) coverage the synthesized beam of the Ooty interferometer has large sidelobes, especially at higher declinations. *By* putting about 20 to 30 small sized antennas as proposed by Swarup and Bagri (1973) it is possible to make an aperture synthesis telescope having a narrow beamwidth of about 15" arc.

However, even to improve the (u,v) coverage of the present interferometer system for a resolution of 40" at least a few more additional antennas are required. In about a year's time it is planned to add two more dishes at intermediate positions to provide sufficient coverage for the low spatial frequency components which will provide a better beam to study the complex structure of radio sources.

APPENDIX 1

GEOMETRICAL RELATIONS FOR A TWO-ANTENNA INTERFEROMETER

In this Appendix we derive the geometrical relations for an interferometer consisting of two antennas P and Q. Let us define the baseline PQ, expressed in RF wavelength λ , as $\overline{B} = \overline{PQ}/\lambda$ and 'h' and 'd' as the hourangle and declination respectively of the pole of the baseline, X, as shown in Fig.Al.1. Let $S_{0}(H_{0}, \delta_{0})$ be the direction of the centre of the field of view under observation. Here H_{O} and \delta_{O} are hour-angle and declination respectively of point S_{0} on the celestial sphere. In Fig.Al.1, θ_0 is the angle between the source direction \overline{PS}_0 and the baseline \overline{PQ} and N is the celestial northpole. Now applying the cosine rule in the spherical triangle NS **o X,** we get declir
phere.
urce d
stial
al tr:
-h) .
will

$$
\cos \theta_{\text{o}} = \sin d \sin \delta_{\text{o}} + \cos d \cos \delta_{\text{o}} \cos(\text{H}_{\text{o}} - h) \tag{A1.1}
$$

The effective baseline for the source at $\texttt{S}\xspace_{\texttt{O}}$ will be B sin Θ _o. We use a Cartesian coordinate system (x,y,z) where z axis is in the direction of the centre of the field of view, S_o, and x and y axes are such that their projections on ground are in the east and north directions respectively. The components of the effective baseline in the x and *y* directions are the components of the spatial

FIG. AI. I. THE SPHERICAL TRIANGLE SHOWING RELATIONS BETWEEN THE POSITIONS OF THE SOURCE S AND THE BASELINE PQ MEETING CELESTIAL SPHERE AT X, N IS THE NORTH POLE. DIRECTION OF THE CENTRE OF THE FIELD OF VIEW UNDER OBSERVATION IS S_0 (SS_O = ρ and ANGLE $NS_0 S = \xi$)

frequency called u and v respectively. If the angle between the effective baseline vector and the *y* axis is σ , the values of u and \mathbf{v} are given by

$$
u = B \sin \theta_0 \sin \sigma , \qquad (A1.2)
$$

and
$$
v = B \sin \theta_0 \cos \theta
$$
. (A1.3)

By application of the sine and cosine rules in the spherical triangle $NS_{\alpha}X$, we get (Rowson 1963)

$$
\sin \sigma \sin \theta_0 = \cos d \sin(\theta_0 - h) \quad , \tag{A1.4}
$$

and cos
$$
\sigma
$$
 sin $\theta_0 = (\sin d - \cos \theta_0 \sin \delta_0)/\cos \delta_0$. (A1.5)

Substituting for cos θ_0 from Eq. (A1.1) in Eq. (A1.5) we get

ccs o sin Θ_{o} = sin d cos δ_{o} - cos d sin δ_{o} cos(H_o-h). (Al.6)

From Fig.Al.l, it is clear that the angle which the baseline PQ makes with the axis of rotation of the earth is $(\pi/2-d)$. Therefore, the components of the baseline parallel and perpendicular to the axis of the earth denoted by $\texttt{B}_{\texttt{1}}$ and $\texttt{B}_{\texttt{2}}$ respectively are given by om Fig.Al.1,
seline \overline{PQ} mak
 $(\pi/2-d)$. Therefore π
rallel and performed by B_1 and B_2
= B sin d,

 B_{1}

(A1.7)

and
$$
B_2 = B \cos d
$$
.

and $B_2 = \vec{B} \cos d$.
Using Eqs.(A1.4) to (A1.8) in (A1.2) and (A1.3) we get

$$
u = B_2 \sin (H_0 - h) , \qquad (A1.9)
$$

and
$$
v = B_1 \cos \delta_0 - B_2 \sin \delta_0 \cos(H_0 - h)
$$
. (A1.10)

For a point source at S_0 , a plane wave will arrive at antenna P, by τ_S seconds later than at antenna Q (see Fig.A1.1) where nd
or
is
Scow
(

$$
\tau_{S_0} = (\lambda/c) \text{ B cos } \theta_0 \text{ seconds.} \qquad (A1.11)
$$

Now we will consider a point source at $S(H, \delta)$ close to $\text{S}_{\text{o}}(\text{H}_{\text{o}}, \text{o}_{\text{o}})$ such that S is p radians away from S_{o} and $\text{S}_{\text{o}}\text{S}$ antenna P, by τ_{S_0} seconds later than at antenna Q (see
Fig.Al.1) where
 $\tau_{S_0} = (\lambda/c)$ B cos θ_0 seconds.
Now we will consider a point source at $S(\text{H},\delta)$ close to
 $S_0(\text{H}_0,\delta_0)$ such that S is p radians away tial pole as shown in Fig.A1.1. For a Cartesian coordinate system with direction cosines (ℓ , m, n) with n along **z** axis PS ₀ and l ,m along x and y axes with their projections on the ground in the east and north directions respectively, from Fig. A.1, we have (Brouw, 1968) an angle ξ with the direction of the north celes-
ole as shown in Fig.Al.l. For a Cartssian coordi-
ystem with direction cosines (ℓ ,m,n) with n along
PS_o and ℓ ,n along x and y axes with their projec-
on the gro nate system with dire
z axis PS_o and l , m altions on the ground :
respectively, from F:
 $l = -\sin \rho \sin \xi$,
and m = sin $\rho \cos \xi$.

$$
\ell = -\sin \rho \sin \xi , \qquad (A1.12)
$$

(A1.13)

111

(A1.8)

From spherical triangle $\text{\sc NSS}^{\vphantom{\dagger}}_{\text{\o}}$, by applying the sine rule we get **c**
 -sin ρ **sin**
 c
 applying t 112

le NSS_o, by applying the sine rule

cos ô sin(H-H₀),

(A1.14)

osine rule twice, we get

$$
\ell = -\sin \rho \sin \xi = \cos \delta \sin(\text{H}-\text{H}_{\text{o}}) \quad , \tag{A1.14}
$$

and by applying the cosine rule twice, *we* get

 $m = sin \rho cos \xi = sin \delta cos \delta_0 - cos \delta sin \delta_0 cos (H-H_0)$ (Al.15)

and by applying the cosine rule tw

m = sin ρ cos ξ = sin δ cos δ -

If S is close to S_o such that ($\delta-\delta$

we can approximate $_{\rm o}$) and (H-H $_{\rm o}$) are small we can approximate and by applying the cosine rule twice, we get
 $m = \sin \rho \cos \xi = \sin \delta \cos \delta_0 - \cos \delta \sin \delta_0 \cos(\mathbb{H}-\mathbb{H}_0)$ (Al.15

If S is close to S_o such that $(\delta-\delta_0)$ and $(\mathbb{H}-\mathbb{H}_0)$ are small

we can approximate
 $\ell \simeq \cos \delta$. $(\mathbb{H}-$

$$
\mathbf{Q} \simeq \cos \delta. \quad (\text{H--H}_{\text{o}}) = \Delta \alpha' \left(\text{say}\right) \tag{A1.16}
$$

 $m \simeq \sin \delta$ cos δ_o - cos δ sin $\delta_o = \sin (\delta - \delta_o) \simeq \delta - \delta_o =$

The time delay for signal to arrive at P with respect to Q from S will be \approx si
 \approx si

he ti

from
 $S = \frac{\lambda}{c}$

here

 $\tau_{\rm S} = \frac{\Lambda}{c}$ B cos θ ,

where θ = angle made by the direction of the source S with the baseline PQ. Thus the difference in delay between signals from S and S_{Ω} B cos θ ,
= angle made by the direction
eline \overline{PQ} . Thus the different
from S and S_o
= λ/c . (B cos $\theta -$ B cos θ_0) B cos θ ,
 θ = angle made by the direction of the source S with

seline \overline{PQ} . Thus the difference in delay between

s from S and S_o

= λ/c . (B cos θ - B cos θ_o), (Al.18)

$$
\tau_S - \tau_S = \lambda/c . (B \cos \theta - B \cos \theta_0) , \qquad (A1.18)
$$

From triangle SS_0X ,

 $\cos \theta = \cos \theta_o \cos \varphi + \sin \theta_o \sin \varphi \cos (\sigma + \xi)$

 $\cos \theta - \cos \theta_0 = \cos \theta_0 (\cos \theta - 1) + \sin \theta_0 \sin \theta$

From triangle SS_0X ,
 $\cos \theta = \cos \theta_0 \cos \theta + \sin \theta_0 \sin \theta \cos (\theta + \xi)$,
 $\cos \theta - \cos \theta_0 = \cos \theta_0 (\cos \theta - 1) + \sin \theta_0 \sin \theta$
 $\cos \theta \cos \xi - \sin \theta \sin \xi$. (A1.19)

Using Eqs.(A1.2), (A1.3), (A1.12), (A1.13) and (A1.19) in Using Eqs.(A1.2), (A1.3), (A1.12), (A1.13) and (A1.19) in $Eq. (A1.18)$ we get **E**
 Al
 T (A1.2), (A1.3), (A1.12)
) we get
= $\frac{\lambda}{c}$ {B[(cos p-1) cos θ Eq.(Al.18) we get
 $\tau_S - \tau_{S_0} = \frac{\lambda}{c} \{B[(\cos \rho - 1) \cos \theta_0]\}$

If ρ is small, $\cos \rho \sim 1$ and we get Using Eqs.(Al.2), (Al.

Eq.(Al.18) we get
 $\tau_S - \tau_{S_0} = \frac{\lambda}{c} \{B[(\cos \theta)]$

If ρ is small, $\cos \theta$
 $\tau_S - \tau_{S_0} = \frac{\lambda}{c} [\mu \ell + \nu m]$

For a baseline of 40

$$
\tau_{S} - \tau_{S_{\circ}} = \frac{\lambda}{c} \{B[(\cos \rho - 1) \cos \theta_{\circ}] + u\ell + \nu m\} \qquad (A1.20)
$$

$$
\tau_{S} - \tau_{S_{\circ}} = \frac{\lambda}{c} \left[u \ell + v m \right] . \tag{A1.21}
$$

 $S_0 = \frac{\lambda}{c}$
 $S_0 = \frac{\lambda}{c}$
 $S_0 = \frac{\lambda}{c}$

baseli For a baseline of 4000 λ and for a source 10' away from the centre of the field of view $(\rho \sim 10')$, the maximum phase error due to the assumption cos $p = 1$ is only 4⁰. For larger value of ρ this correction may become appreciable. As the Ooty interferometer has about 2°5 field of view in the east-west direction and has a baseline of about 4000λ , this error may become appreciable for sources away from centre of field of view. With the approxi-

with the state of the company

$$
\tau_{S} - \tau_{S} = \lambda/c \left[u \Delta \alpha' + v \Delta \delta \right].
$$

 $(A1.22)$

APPENDIX 2

_BASELINE PARAMETERS OF A TWO-ANTENNA INTERFEROMETER

In this Appendix we derive expressions for the baseline parameters B_1 , B_2 and h in terms of the measured coordinates of the antennas. Here B_1 and B_2 are components of the baseline B parallel and perpendicular to the axis of rotation of the earth respectively and expressed in units of RF wavelength and h is hour-angle of the pole of the baseline \overline{B} . The vector \overline{B} is formed by the line joining the two antennas $P(x_1, y_1, p_1)$ and $Q(x_2,y_2,p_2)$. Cartesian coordinate system (x,y,p) with axes along east, north and zenith respectively is used in the survey of the location of the antennas.

Let us define N as the north celestial pole, z as the zenith direction, X as the direction of the pole of the baseline \overline{PQ} and φ as the geographic latitude of antenna P , as shown **in Fig.** A2.1. We first find values of the azimuth angle A and zenith angle z of the baseline PQ. These are given by Let us define N as the north celestial pole,

z as the zenith direction, X as the direction of the pole

of the baseline \overline{PQ} and φ as the geographic latitude of

antenna P, as shown in Fig. A2.1. We first find v of the baseline \overline{PQ} and φ as the geographic latitude of
antenna P, as shown in Fig. A2.1. We first find values
of the azimuth angle A and zenith angle z of the baseline
 \overline{PQ} . These are given by
tan $A = (x_2-x$

$$
\tan A = (x_2 - x_1)/(y_2 - y_1), \qquad (A2.1)
$$

From the spherical triangle NZX, the declination d and hour-angle h of the pole X are given by From the spherical triangle
nation d and hour-angle h of the pole
sin d = sin φ cos z + cos φ sin z cos A ,
and cos h = (cos z - sin φ sin d)/cos φ of From the spherical triangle NZX, that
ion d and hour-angle h of the pole X are
sin d = sin φ cos z + cos φ sin z cos Λ ,
and cos h = (cos z - sin φ sin d)/cos φ cos d.
To find B₁ and B₂, we first fin

$$
\sin d = \sin \varphi \cos z + \cos \varphi \sin z \cos A , \qquad (A2.3)
$$

To find B_1 and B_2 , we first find projection of PQ on the plane containing *y* and p axes, called PN, and the angle β which the line PN makes with the y-axis. We get To find B_1 and

of PQ on the plane containi

the angle β which the line

get

PN = $[(y_2-y_1)^2 + (p_2-p_1)^2]^{\frac{1}{2}}$

and tan $\beta = (p_2-p_1)/(y_2-y_1)$
 B_1 is obtained by taking pr

the axis of rotation of the

$$
PN = [(y_2 - y_1)^2 + (p_2 - p_1)^2]^{\frac{1}{2}}, \qquad (A2.5)
$$

 $(A2.6)$

 B_{1} is obtained by taking projection of the line PN along the axis of rotation of the earth, which is inclined at an angle φ to the y-axis. Thus, we get

$$
B_1 = \lambda^{-1} [(\text{PN} \cos(\beta - \varphi))]. \qquad (A2.7)
$$

 $B₂$ is ⊷btained by taking the vector sum of the component of PN perpendicular to the axis of rotation of the earth and the x-component of the line PQ. Thus, *we* get

$$
B_2 = \lambda^{-1} \cdot \left[(PN)^2 \sin^2 (\beta - \varphi) + (x_2 - x_1)^2 \right]^{\frac{1}{2}} \,. \tag{A2.8}
$$

APPENDIX 3

ALLOWABLE ONE-WAY PATH LOSS FOR A CLOSED LOOP SYSTEM

In this Appendix we briefly review the limitations on the allowable path attenuation for a closed loop system in which the reference or correction signal at any point along the path is formed by combining the two signals travelling in opposite directions. The permissible attenuation depends upon the allowable phase error of the resultant reference or correction signal. Here we calculate the phase errors that arise due to the receiver and oscillator noise. The phase errors due to the presence of reflections on the transmission path have been discussed by Swarup and $\text{Yang}(1961)$ and Jones (1972). The contribution by oscillator noise is particularly influenced by the effect of the reflection coefficient P and the use of a multiplier which has a finite value of the proportionality constant ε . ε is defined as the ratio of the amplitudes of second harmonics, due to signal at any port, to the product of the two input signals.

Let S_1 at frequency $(\omega_0/2 + \omega_2)$ and S_2 at frequency $(\omega_0/2)$ be the power outputs of the two oscillators at home and remote stations respectively; N_1 and N_2 be their noise power density per Hz, kT per Hz be the receiver noise, and $\beta_1 \& \beta_3$ be the fractions of power coupled to the multiplier from the oscillator at home station and the signal αS ₂ coming from remote station respectively. The signals at the

two inputs of the multiplier are X and Y. These are shown in Fig.A3.1. Also, let B_1 , B_2 and B_3 be the equivalent bandwidths in Hz of the receiver IF, output filter and the oscillator noise respectively, as shown in Fig.A3.2. The output of the multiplier is given by

 V_{\circ} = XY+ ε (X²+Y²)

The desired reference signal at frequency $(\omega_0 + \omega_2)$ in case of the sum frequency system, and at ω_{α} in case of the difference frequency system, is formed by multiplying signals $\beta_1 S_1$ from home station and $\alpha\beta_3 S_2$ from remote station. This can be written as

$$
S = (\alpha \beta_3 \beta_1 S_2)^{\frac{1}{2}}.
$$
 (A3.2)

The phase errors are caused by the noise components present in the output of the multiplier over the bandwidth B_2 . The noise terms are produced by the multiplication of the individual terms of the inputs X and Y (excluding signal S defined above), and ε times the second harmonics of the two inputs. We assume that the signal $\beta_1 S_1$ from home station is strong such that

the product due to $\beta_1 N_1$ and $\rho^2 \beta_3 N_1$ over B_2 is larger (i) than the product due to $\beta_1 N_1$ and $\rho^2 \beta_3 N_1$ over B_3 .i.e. $(2N_1B_2S_1)^{\frac{1}{2}} > N B_3$ and (ii) the product due to $\beta_1 S_1$ and kT/Hz over B_2 is larger

 $(A3.1)$

BLOCK DIAGRAM SHOWING SIGNAL AND NOISE FIG. A3.1 COMPONENTS AT VARIOUS STAGES FOR CALCULATING ALLOWABLE ONE WAY PATH LOSS FOR A CLOSED LOOP SYSTEM

SPECTRAL DISTRIBUTION OF VARIOUS SIGNAL AND NOISE COMPONENTS

than the product of the receiver noise at the inputs over B_1 **i.e.** $(2\beta_1 S_1 B_2)^{\frac{1}{2}} > (kT)^{\frac{1}{2}}B_1$.

Generally $S_1 \gg N_1B_3/B_2$ and therefore the terms due to noise along with $\beta_1 S_1$ (i.e. $\beta_1 N_1$) on one side and receiver noise (i.e. kT) or signal αS_2 on other side will be negligible in comparison with the product of $\beta_1 S_1$ and kT/Hz, all over B_2 . Therefore, the output signal to noise ratio can be approximated by Generally $S_1 \gg N_1 B_3/B_2$

e along with $\beta_1 S_1$ (i.e. β

ise (i.e. kT) or signal α

le in comparison with the

over B_2 . Therefore, the

e approximated by
 $\frac{1}{2}$ $(\alpha S_2 \beta_3)^{\frac{1}{2}}$
 $(\alpha S_2 \beta_1)^{\frac{1}{2}} + (4 \beta$

$$
\frac{S}{N} \simeq \frac{\frac{1}{2} (\alpha S_2 \beta_3)^{\frac{1}{2}}}{(2kTB_2)^{\frac{1}{2}} + (4\beta_3 \rho^2 N_1 B_2)^{\frac{1}{2}} + (4\epsilon \beta_1 N_1 B_2)^{\frac{1}{2}}}
$$
\n(A3.3)

Here in the denominator the first term is due to the receiver noise, the second term is due to the reflections on the line and the last term is due to non ideal multiplier. For practical values of receiver temperature 10^{3} ^OK, $\text{N}_1/\text{S}_1 \simeq 10^{-14}$ at a few kHz away from the line frequency $\omega_0/2$ or $(\omega_0/2 + \omega_0);$ $\rho = 0.01, \varepsilon = 10^{-3}$, $\beta_1 = 10^{-3}$, $\beta_3 = 1$, oscillator power of 1 Watt and $B_2 = 10$ Hz, it can be shown that the contribution due to the receiver noise is much smaller than that due to the reflections and the non ideal behaviour of the multiplier. For a rms phase error of 6° the output signal to noise ratio should be greater than 20 dB, which implies that $\beta_{1} = 10^{-3}$, $\beta_{3} = 1$, oscillato
it can be shown that the con
noise is much smaller than t
and the non ideal behaviour
rms phase error of 6⁰ the ou
should be greater than 20 dB
 $\frac{S}{N} \approx \frac{(\alpha S_{2} \beta_{3})^{\frac{1}{2}}}{(4\beta$ ¹

it can be shown that the contribution due to the receiver

noise is much smaller than that due to the reflections

and the non ideal behaviour of the multiplier. For a

rms phase error of 6[°] the output signal to no

$$
\frac{S}{N} \simeq \frac{(\alpha S_2 \beta_3)^{\frac{1}{2}}}{(4\beta_3 \rho^2 N_1 B_2)^{\frac{1}{2} +} (4\epsilon \beta_1 N_1 B_2)^{\frac{1}{2}}} > 10
$$
 (A3.4)

When two oscillators are used at the two ends of the transmission path the maximum loss for the above assumed values works out to be about 140 dB. However, when the signal from the remote end is formed by reflection of the incident signal (reflected modulation technique) the maximum allowable one-way path loss has to be limited to about 70 dB. These limits are mainly due to reflections on the transmission path, the non ideal behaviour of the multiplier and presence of noise in the oscillator output.

REFERENCES

- Ambartsumian,V.A. 1971, in Nuclii of Galaxies, ed. O'connell, D,J.K., (Amsterdam, North-Holland Publishing Co.).
- Baars,J.W.M., Frederik,J.Vander Bergge, Casse,J.L., Hamaker, J.P., Sondaar, L.H., Vissar, J.J., and Wellington, K.J. 1973, Proc. I.E.E.E., 61, 1258.
- Basart, J.P., Miley, G.K., and Clark, B.G. 1970, I.E.E.E. Trans., AP-18, 375.

Berge,G.L. 1966, Ap.J., 146, 767.

Blum, E.J. 1959, Annales d'Astrophysique, 22, 140.

Bracewell, R.N. 1965, The Fourier Transform and Its Applications, (New York, mc Graw-Hill.).

Branson, N.J.B.A. 1968, M.N.R.A.S., 139, 155.

- Brouw, W.N. 1968, Astronomical Observatory, Leiden, Internal Report,SRTP-ITR-62.
- Brouw,W.N. 1971, Ph.D. Thesis, Univ. Leiden, Netherlands.

Christiansen,W.N. 1973, Proc. I.E.E.E., 61, 1266.

- Christiansen,W.N., and Hogbom,J.A. 1969, Radiotelescopes, (London, Cambridge Univ. Press).
- Christiansen, W.N., and Warburton, J.A. 1955, Australian J. Phys., 8, 474.
- Douglass,J.N., Bash,F.N., Ghigo,F.D., kosley,G.F., and Torrence, G.W. 1973, A.J., 78, 1.

Downes,D., and Martin,A.H.M. 1971, Nature, 233, 112.

Drake,F.D.,and Hvatum,S. 1959, A.J., 64, 1163.

Elsmore, B., Kenderdine, S., and Ryle, M. 1966, M. N. R. A.S., 134, 87.

Elsmore, B., and Mackay, C.D. 1969, M.N.R.A.S., 146, 361.

Fomalont, E.B. 1973, Proc. I.E.E.E.,.61, 1211.

Fomalont, E.B., and Moffet, A.T. 1971, A.J. 76 , 5.

Fomalont,E.B., and Wright,C.H. 1974, in Galactic and Extragalactic Radio Astronomy, ed. Verschuur,G.L., and Kellermann,K.I. (New York, Springer-Verlag Inc.).

Frater, R.H. 1964, Rev. Sci. Instr. 35, 810.

Copal-Krishna and Swarup,G. 1975, Astrophys. Letters, in press.

Gruppo Roub 1968, Contribution of the L.N.R.E. No.51.

Gulkis,S. 1970, Radio Science, 2, 505.

Hamakar,J.P. 1973, Astronomical Observatory, Leiden, Internal Report, SRTP-ITR-109.

Hinder, R., and Ryle, M.1971, M.N.R.A.S., 154, 229.

Jones, I.G. 1972, Ph.D. Thesis, Univ. Sydney, Australia.

Kapahi,V.K. 1969, Unpublished.

Kapahi,V.K.,'Damle,S.H., Balasubramanian,V., and Swarup,G. 1975, J. Inst. Electron. Telecom. Engrs., 21, 117.

Komesaroff, M.M. 1960, Austr. J. Phys., 13, 153.

Kraus, J.D. 1966, Radio Astronomy, (New York, McGraw-Hill).

Kundu, M.R. 1959, Annales d'Astrophysique, 22, 1.

Little, A.G., and Payne-Scott, Ruby. 1951, Austr. J. Sci. Res., 4, 489.

Longair, M.S., Malumian, V.H., and Sargent, W.C.W. 1970, Ap. Letters, 7, 23.

Markarian, B.Y. 1967, Astrofisika, 3, 55.

Markarian,B.Y. 1969a, Astrofisika, <u>5</u>, 443.

Markarian,B.Y. 1969b, Astrofisika, <u>5</u>, 581.

Markarian, B.Y., and Lipovetsky, V.A. 1971, Astrofisika, 511.

Markarian,B.Y , and Lipovetsky,V.A. 1972, Astrofisika, $8, 155.$

Mc Adam,W.B. 1966, Planet, Space. **Sci.,** 14, 1041.

McCready, L.L., Pawsey, J.L., and Payne-Scott, R. 1947, Proc. Roy. Soc. (London), 1904, 357. Mills, B.Y., Aitchison, R.E., Little, A.G., and McAdam, W.B. 1963, Proc. I.R.E.E. (Australia), 24, 156. Morimoto, M., and Labrum, N.R. 1967, Proc. I.R.E.E. $(A$ ustralia), 28 , 352. Morris, D., and Berge, G.L. 1962, Ap.J., 136, 276. Peterson, S.D. 1973, A.J., 78, 811. Pooley, G.G., and Ryle, M. 1969, M.N.R.A.S., 139, 515. Radhakrishnan,V., and Roberts,J.A. 1960, Phys. Rev. Letters, 4 , 493. Read, R.B. 1961, I.R.E. Trans., AP-9, 31. Roberts, J.A., and Ekers, R.D. 1966, Icarus, 5 , 149. Roberts,J.A., and Ekers,R.D. 1968, Icarus, 8,160.. Roberts, J.A., and Komesaroff, M.M. 1965, Icarus, 4 , 127. Rowson, B. 1963, M.N.R.A.S., 125, 177. Ryle, M. 1952, Proc. Roy. Soc. (London), 2114, 351. Ryle,M. 1972, Nature, 239, 435. Ryle, M., and Hewish, A. 1960, M.N.R.A.S., 120, 220. Sandqvist, A. 1971, Ph.D. Thesis, Univ. Maryland, USA. Sarma, N.V.G., Joshi, M.N., Bagri, D.S., and Ananthakrishnan.S. 1975, J. Inst. Electron. Telecom. Engrs., 21 , 110. Sheridan, K.V., Labrum, N.R., and Payten, W.J. 1973, Proc. I.E.E.E., 61, 1312. Sloanker, R.M. 1959, A.J., 64, 346. Smith,E.J., Davis,L.Jr., Jones,D.E., Coleman,P.J., Colburn,D.S., Dyal,P., Sonett,C.P. 1975, Science, 188, 451. Sramek,R.A., and Tovmassian,H.M. 1975, $Ap.J.J.J.$, 196, 339.

Swarup, G., and Bagri, D.S. 1973, Proc. I.E.E.E., 61,1285.

Swarup,G., Sarma,N.V.G., Joshi,M.N., Kapahi,V.K., Bagri,D.S., Damle,S.H., Ananthakrishnan,S., Balasubramanian,V., Bhave,S.S., and Sinha,R.P.1971, Nature Phys. Sci., 230, 185.

Swarup,G., and Yang,K.S. 1959, Wescon Convention Record, pt.1, 17.

Swarup, G., and Yang, K.S. 1961, I.R.E. Trans., $AP-9$, 75.

Swenson, G.W., and Mathur, N.C. 1968, Proc. I.E.E.E., $56, 2114$.

Thomasson, P_1 , and Malumian, $V.H. 1973$, $M.N.R.A.S., 168$, 295.

Thompson,M.C., Wood,L.E., Smith,D., and Grant,W.B. 1968, I.E.E.E. Trans.,AP-16, 683.

Tovmassian, H.M. 1966, Austr. J. Phys., 19 , 565.

Tovmassian, H.M. 1972, A.J., 77, 705.

Veron, M.P., Veron, P., and Witzel, A. 1974, Astron. Astrophys. Suppl. 13, 1.

Von Hoerner, S. 1961, Publ. NRAO, 1 , No.19.

The VLA (1967): A proposal for a Very Large Radio telescope. National Radio Astronomy Observatory,USA, internal Report, Vol.I and Vol.II.

Wade, C.M. 1970, Ap.J., 162, 381.

Whiteoak, J.B., Rogstad, D.H., and Lockhart, I.A. 1974, Astron. Astrophys., 26, 245.

Wild, J.P. (ed). 1967, Proc. I.R.E.E. (Australia), 28, No.9.